

# Mask Assignment and Synthesis of DSA-MP Hybrid Lithography for sub-7nm Contacts/Vias

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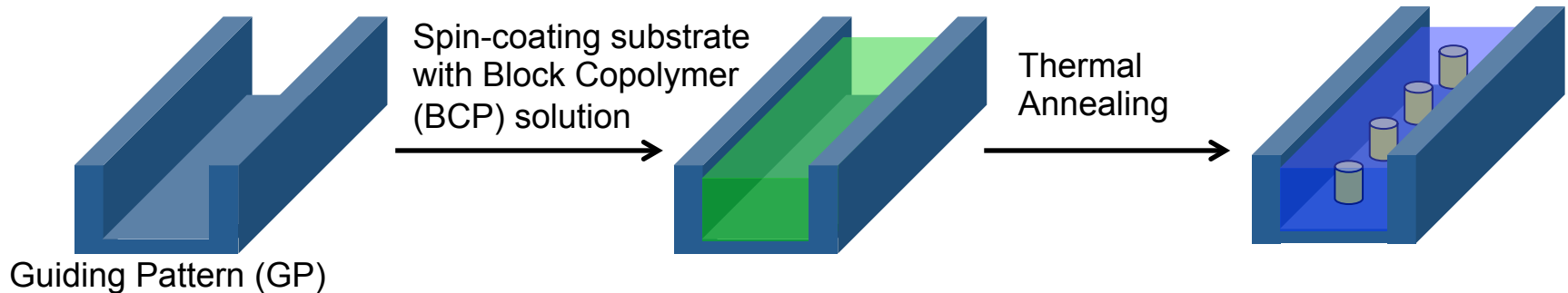
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<http://impact.ee.ucla.edu>

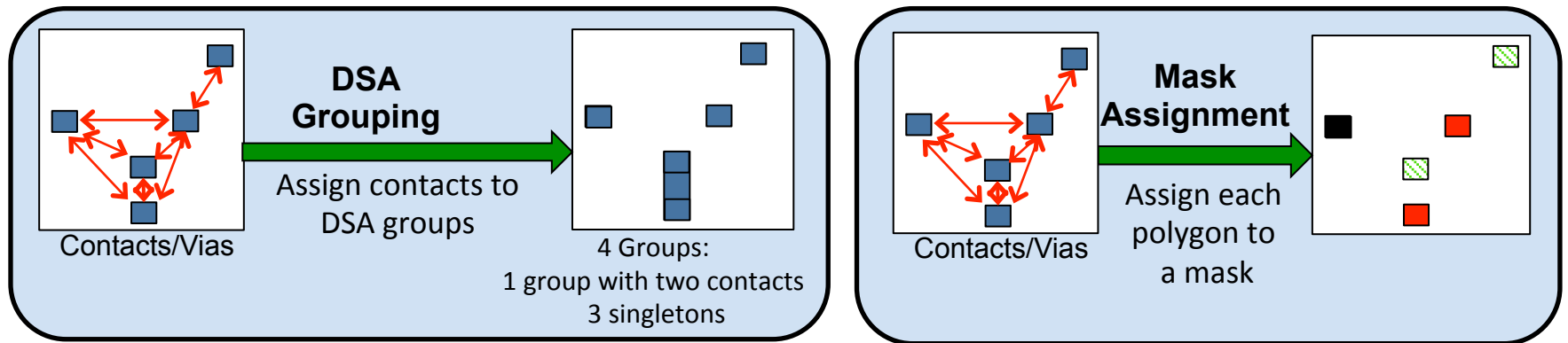
# Motivation

- Directed Self Assembly (DSA) is a strong candidate for future technology nodes

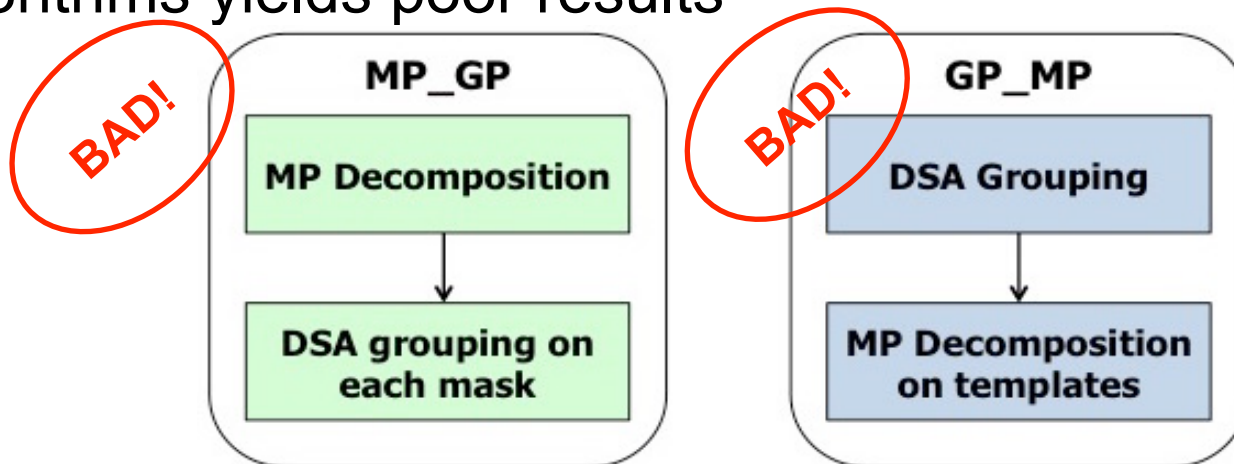


- BUT** Pure DSA can not achieve 7nm node or beyond
  - Because resolution required for GP can not be delivered by 193i lithography
  - Challenges in finding BCPs which can achieve that small pitch
- Integration of **DSA** with **Multiple Patterning (MP)** is attractive for sub-7nm
  - Reduce number of masks → less costly process
  - Potentially more flexibility in polygon sizes

# DSA Grouping and Mask Assignment

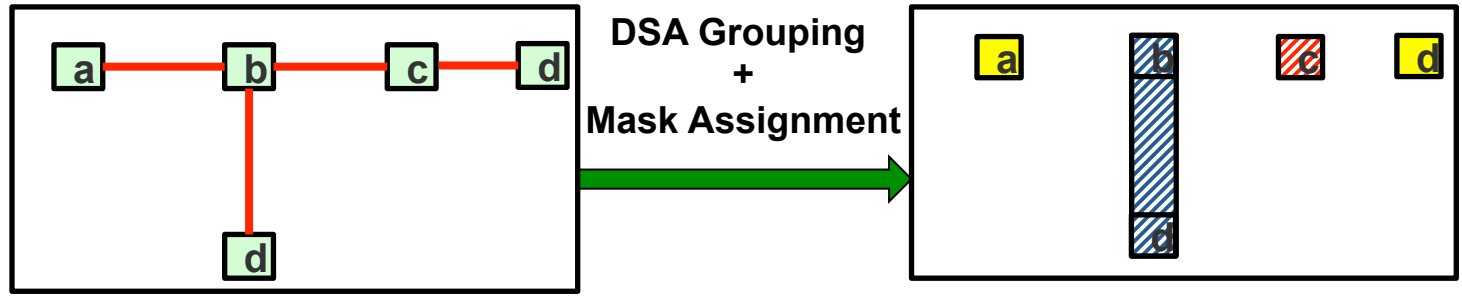


- Previous work (*Badr et al; SPIE'15*) showed that cascading existing DSA grouping and MP decomposition algorithms yields poor results



# This Work

Objective  
of this  
work



## Contribution

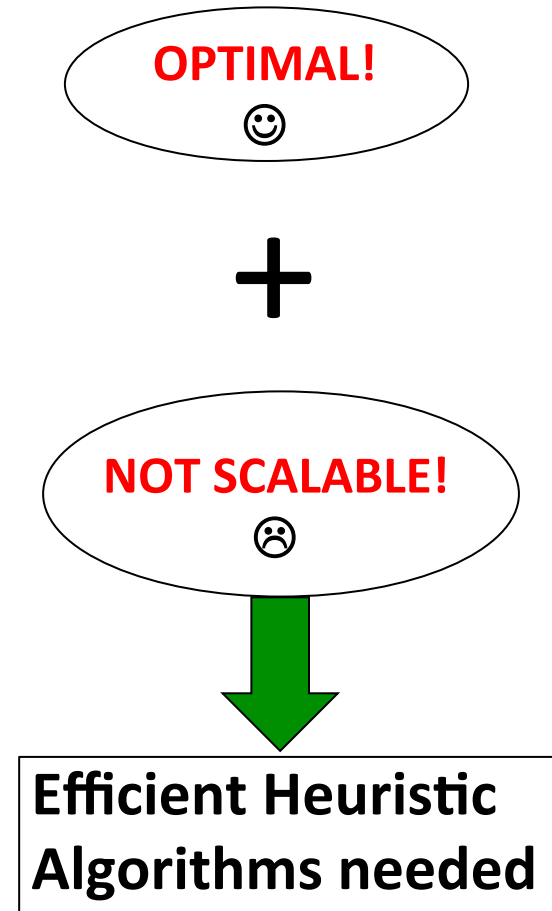
**Optimal ILP**

Benchmark against

**Graph-based  
Heuristic**

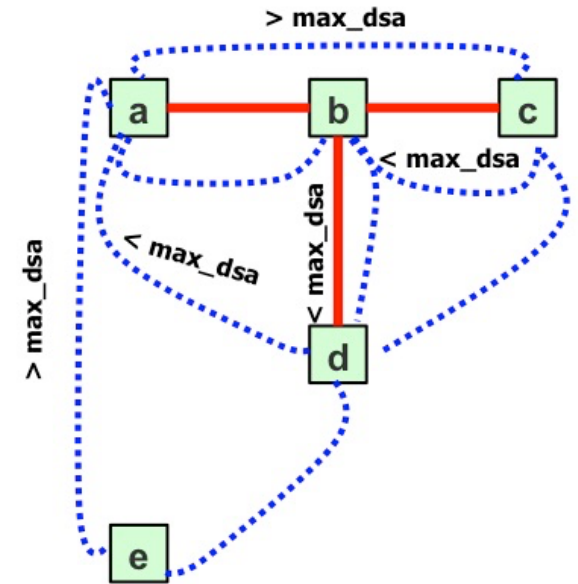
# Integer Linear Programming (ILP) Formulation

- Objective: minimize number of conflicts
  - A conflict is when two contacts with inter-distance  $<$  litho\_dist are
    - on same mask and
    - not in same DSA group
- Constraints [Simplified]:
  - Two “close” contacts are assigned to different masks or same DSA group if possible
  - Number of contacts in each group  $\leq$  max\_g
- ILP works for DP, TP, QP, and any number of masks that is power of two.



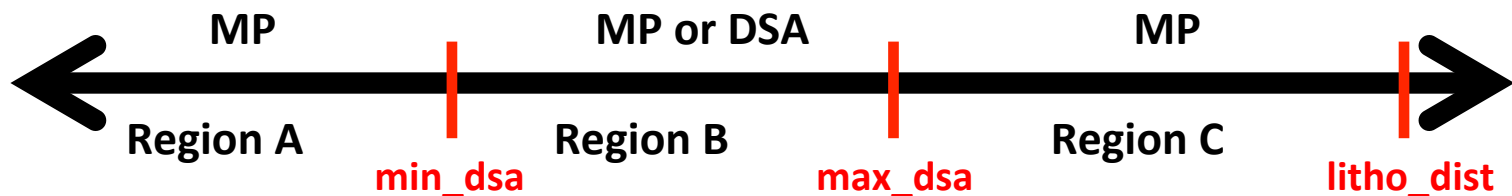
# Hybrid Graph Representation

1. **Spacing Edge**: between every pair of contacts within *litho\_dist*
2. **Grouping Edge**: between every pair of neighboring contacts that can be DSA-grouped
  - $min\_dsa \leq distance \leq max\_dsa$
  - Collinear, on same y or x axis
    - To have 193i-manufacturable templates



Blue: Spacing Edge  
Red: Grouping Edge

Ranges of Distance between two polygons where spacing violation can be resolved by MP or DSA

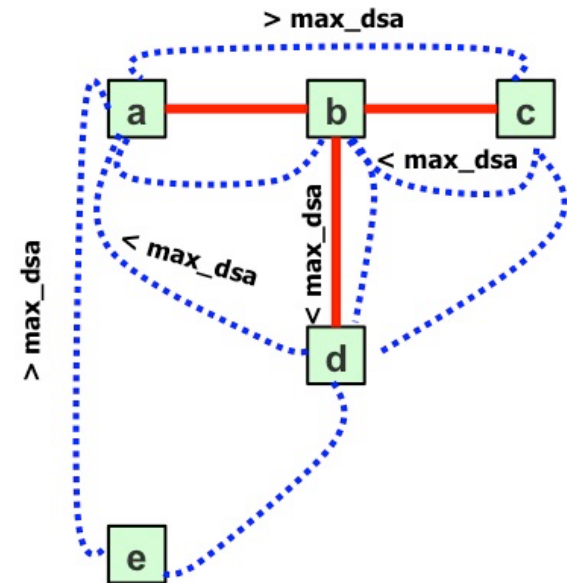


# Proposed Heuristic

- Maximize chance of DSA grouping → maximize possibility of eliminating conflicts
- Find max number of grouping edges with no common nodes

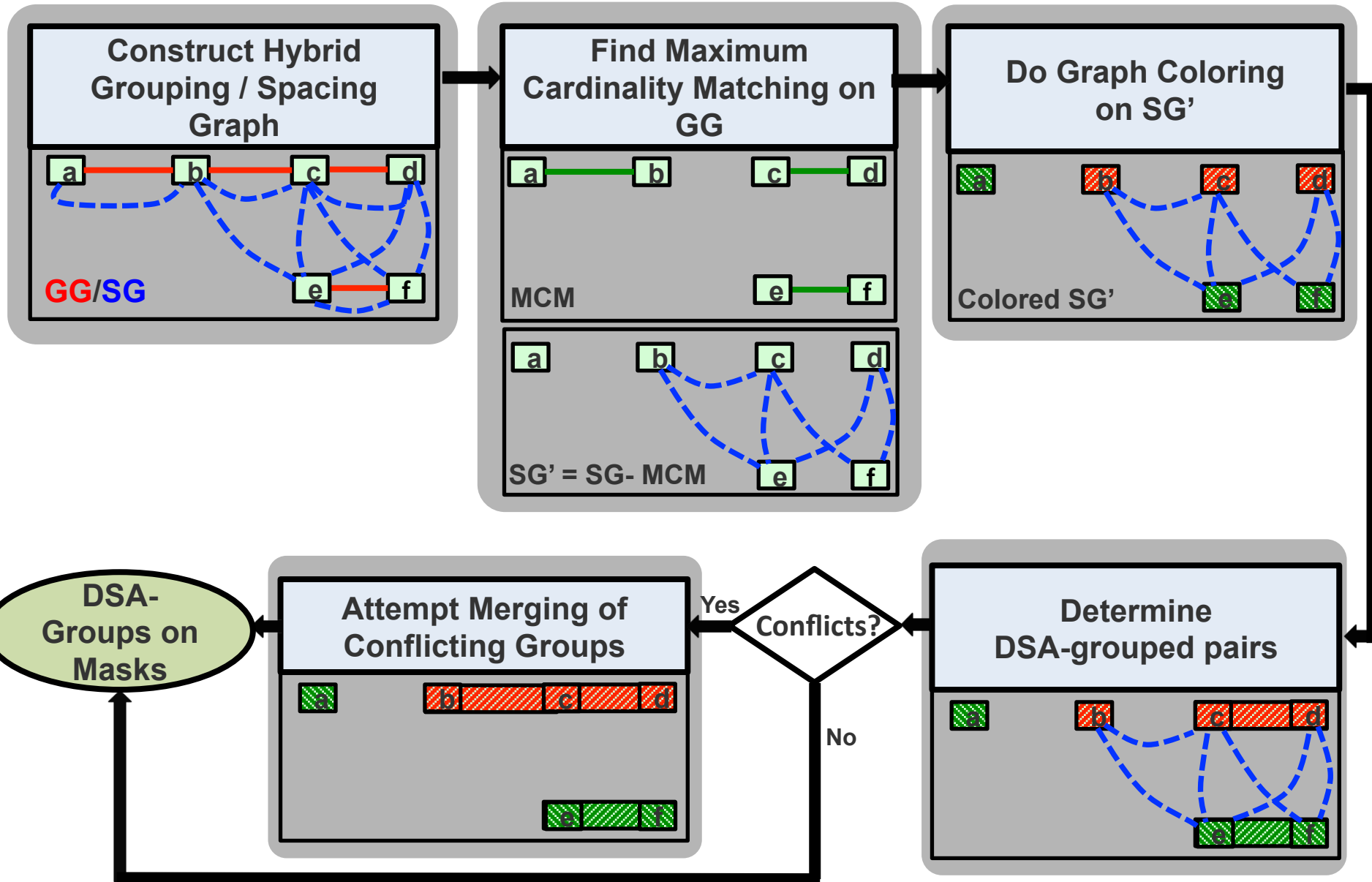
**Maximum Cardinality  
Matching  
(MCM)**

Can be solved in polynomial time!



Blue: Spacing Edge  
Red: Grouping Edge

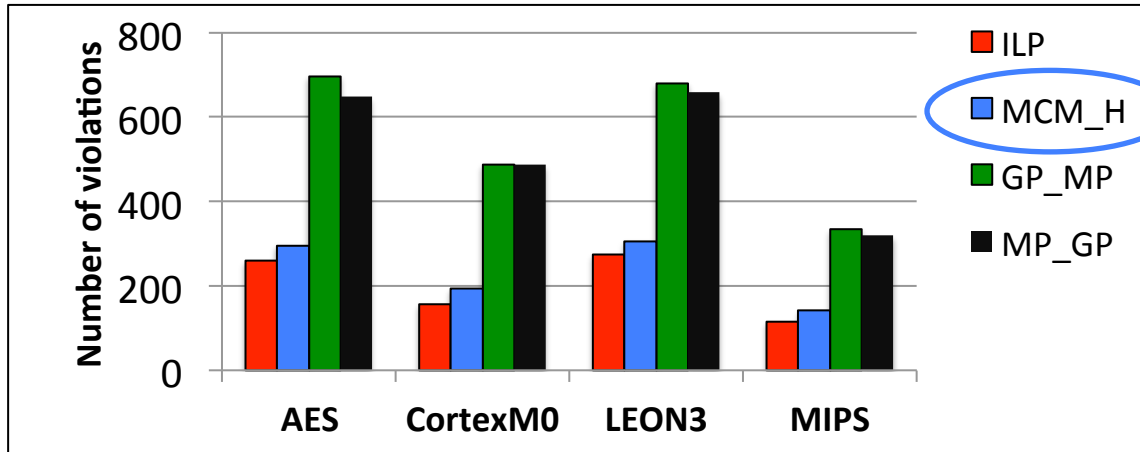
# Proposed Heuristic Algorithm: MCM\_H



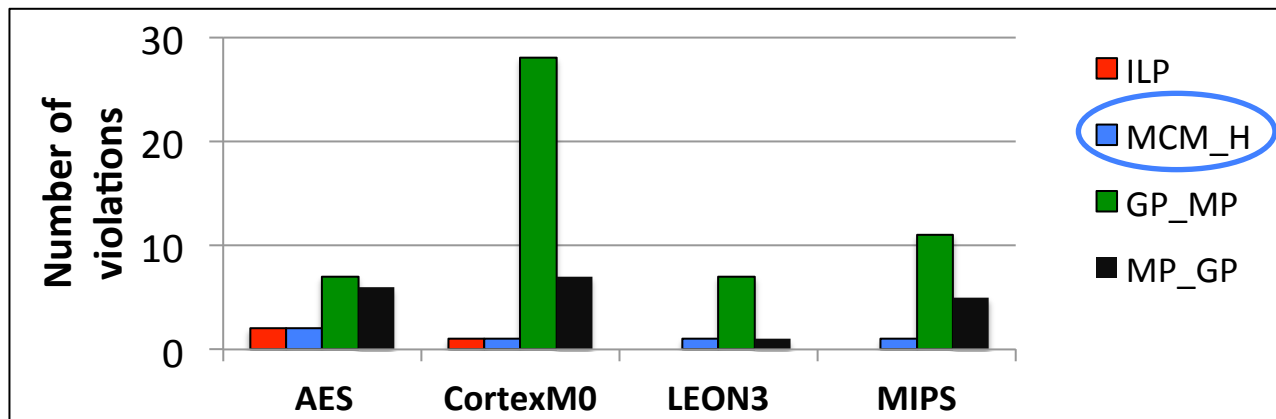


# Results

N=2 (DP)



N=3 (TP)



Test case	Number of Vias
AES	48123
CortexM0	35255
LEON3	93474
MIPS	34784

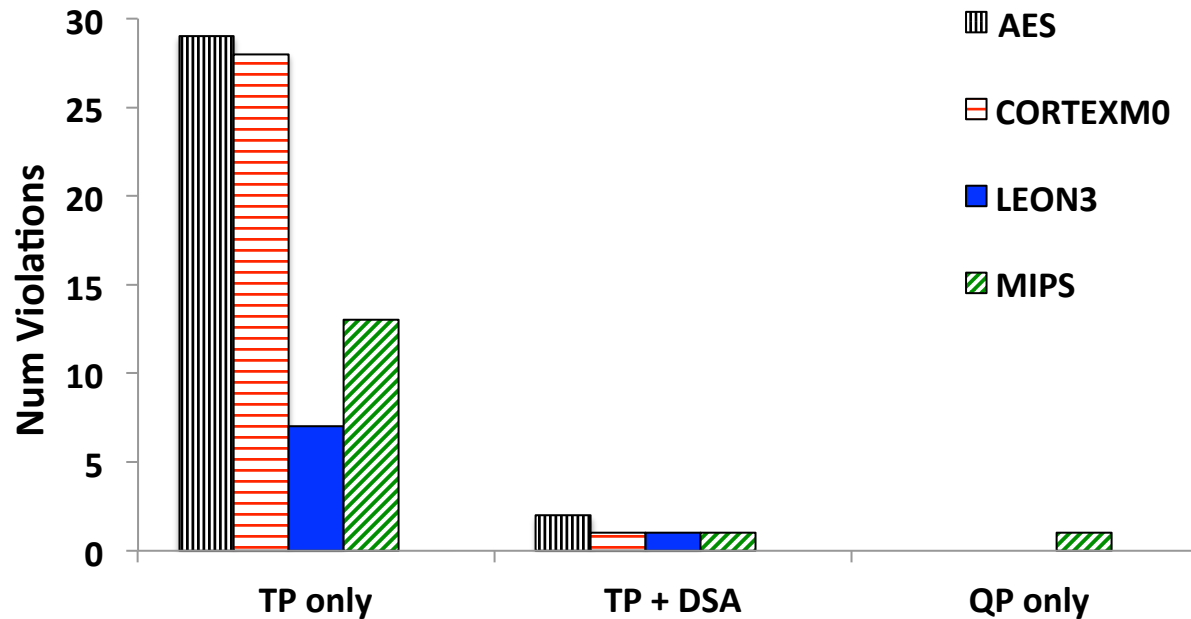
MCM\_H is ~200x faster than ILP. (Max runtime on our test cases is 13s.)

MCM\_H has 16.3% more violations than ILP.

MCM\_H has 56% fewer violations than sequential approaches (GP\_MP & MP\_GP)

# Can we really reduce one mask?

Number of violations with TP only, TP+DSA using MCM\_H and QP only



# Conclusion

- We proposed optimal ILP formulation to solve the simultaneous DSA grouping + MP decomposition problem for a hybrid DSA-MP process.
- We presented an efficient graph-based heuristic (MCM\_H).
- MCM\_H produces 16.3% more violations than ILP, but is ~200x faster.
- MCM\_H produce 56% fewer violations than naïve sequential approaches which cascade grouping and decomposition.

# Future Work

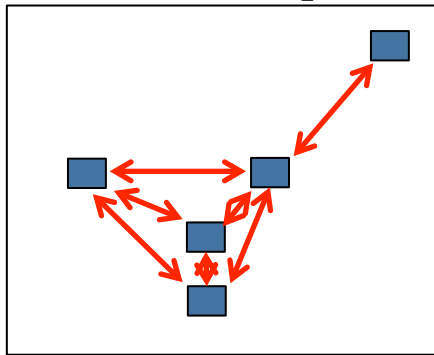
- Explore different MP+DSA integration schemes.
- Allow more flexible grouping enabled by EUV or more restricted due to Sidewall image transfer e.g. SAQP.

**THANK YOU!**

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**BACKUP**

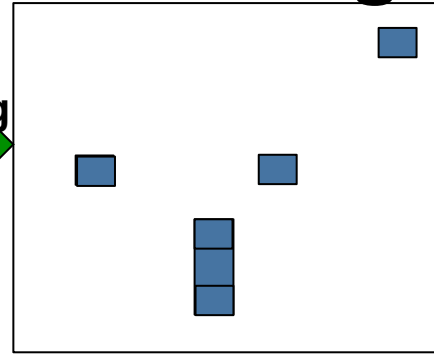
# DSA Grouping and Mask Assignment



Contacts/Vias

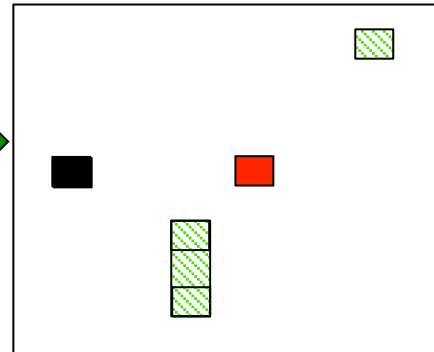
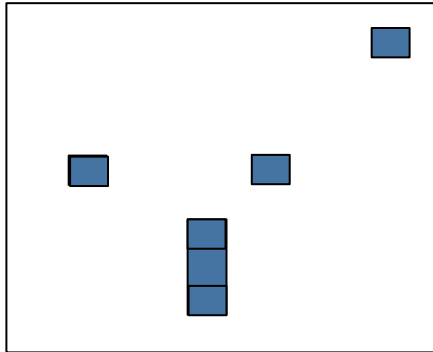
**DSA Grouping**

Which contacts are printed using the same template

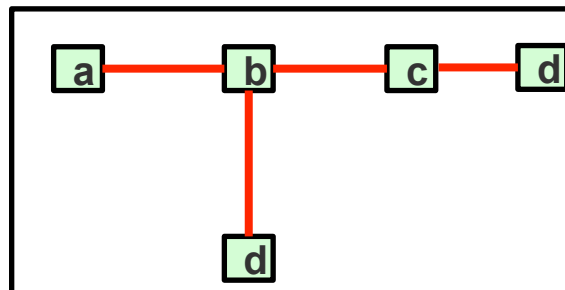


4 Groups: 1 group with two contacts and 3 singletons

**Mask Assignment**

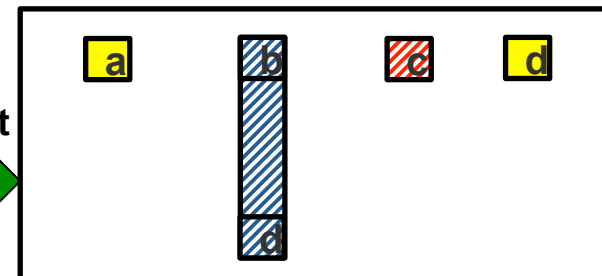


**Objective of this work**



Contacts/Vias

**DSA Grouping + Mask Assignment**



# Hybrid DSA-MP Process

## Important Parameters and Rules

**N**

Number of masks

**litho\_dist**

Min allowed space  
on a mask

**min\_dsa**

Min distance  
between two contacts  
in a DSA groups

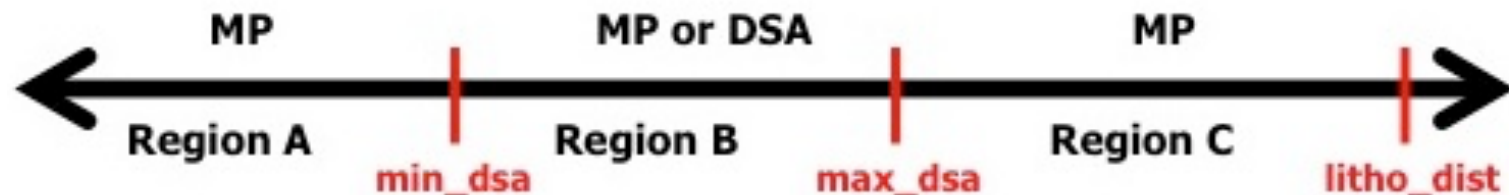
**max\_dsa**

Max distance  
between two  
neighboring contacts  
in one DSA group

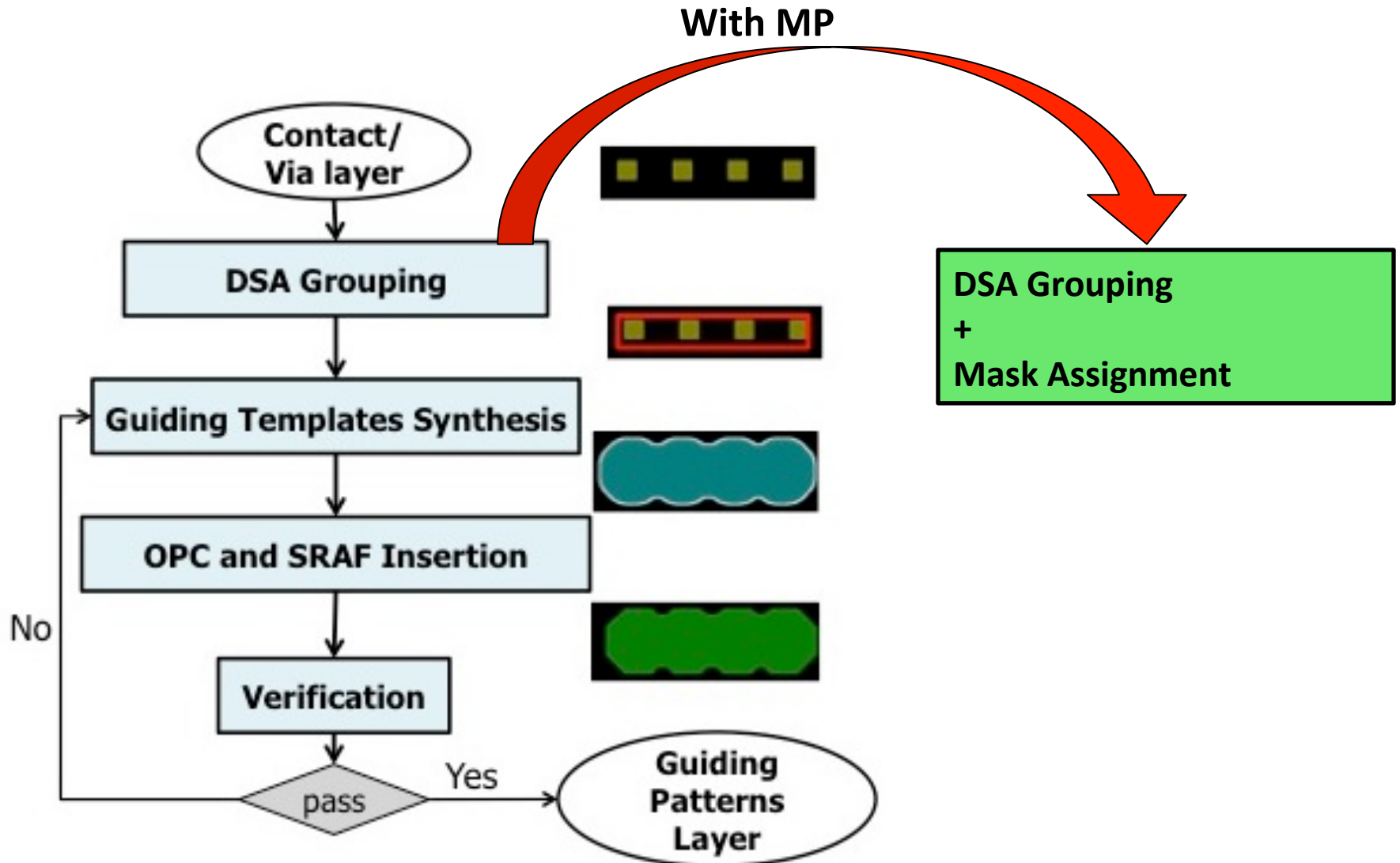
**max\_g**

Maximum number  
of contacts  
in a single DSA group

Ranges of Distance between two polygons where spacing violation can be resolved by MP or DSA

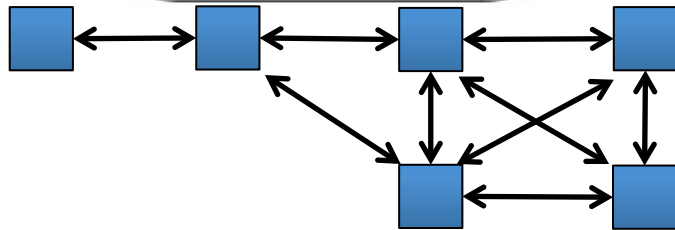
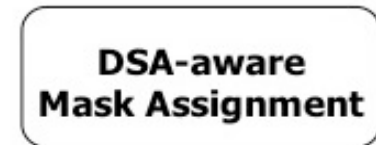
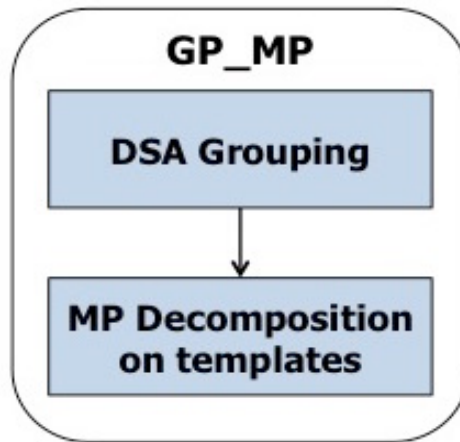
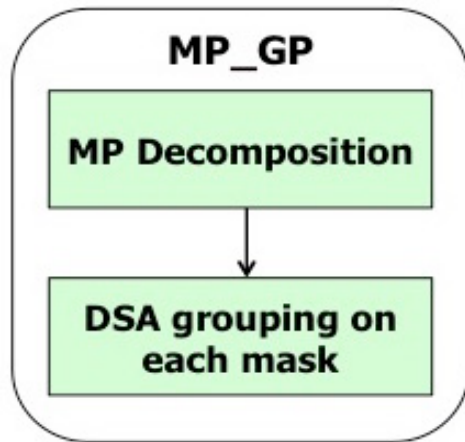


# CAD flow for DSA

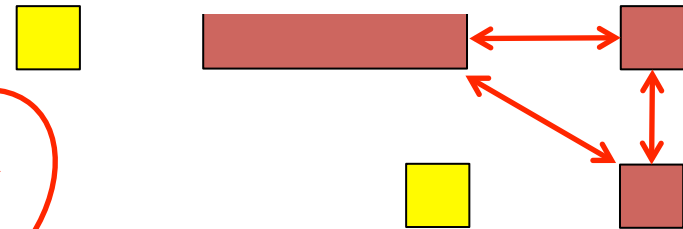




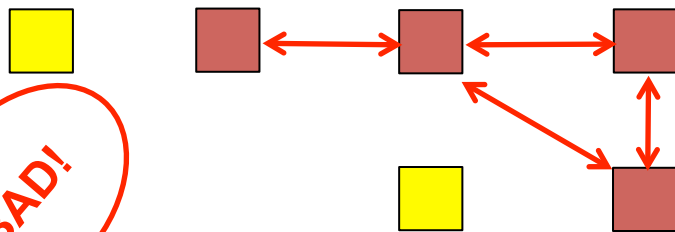
# Alternative Flows



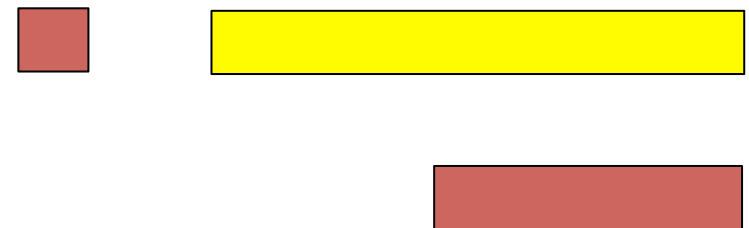
Original Snippet.



Result of MP\_GP, N=2.  
The marker shows a spacing violation.



Result of GP\_MP, N=2.  
The marker shows a spacing violation.



Conflict-free  
Grouping & Decomposition, N=2.

# Experiments and Results

- Test cases have been synthesized, placed and routed using commercial 45nm SOI libraries, then scaled and sized
- Used via1 layer. After scaling: min space=21nm, via width=14nm
- Implemented in C++, using Boost library, OpenAccess
- Used Calibre Multi-patterning tool

Number of vias in test cases

Test case	Number of Vias
AES	48123
CortexM0	35255
LEON3	93474
MIPS	34784

Parameters used in experiments

<i>min_dsa</i>	20
<i>max_dsa</i>	42
<i>litho_dist</i>	66
<i>max_g</i>	2
<i>contact width</i>	14
$L_0$	34
$N$	2 (DP) and 3(TP)